Unified Engineering Problem Set Week 7 Spring, 2008

Lectures: M11, M12 Units: M4.6

M7.1 (15 points) An aluminum rod has a solid circular cross-section with a 20-cm diameter and is 3 meters in length. The rod is clamped to a solid wall at one end, and is subjected to a distributed negative torque of linearly increasing intensity: from 0 at the wall to 100 N-m/m at the tip. There also is a concentrated positive torque of 200 N-m at the midpoint of the rod. The configuration is shown below. The modulus of aluminum is 67 GPa and the Poisson's ratio is 0.3.

Cross-Section



- (a) Determine the torque distribution in the rod structural configuration and sketch this as a function of x_1 .
- (b) Determine the twist at the tip of the rod.
- (c) Determine the maximum shear stress in the rod and its location.
- (d) If the rod were a hollow tube with the same outer radius and a wall with a thickness of 20 mm, how would these answers change?